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Phase effect of a general two-Higgs-doublet model in $b \rightarrow s \gamma$

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In a general two-Higgs-doublet model (2HDM), without the *ad hoc* discrete symmetries to prevent tree-level flavor-changing-neutral currents, an extra phase angle in the charged-Higgs-fermion coupling is allowed. We show that the charged-Higgs amplitude interferes destructively or constructively with the standard model amplitude for $b \rightarrow s \gamma$ depending crucially on this phase angle. The popular models I and II are special cases of our analysis. As a result of this phase angle the severe constraint on the charged-Higgs-boson mass imposed by the inclusive rate of $b \rightarrow s \gamma$ from CLEO can be relaxed. We also examine the effects of this phase angle on the neutron electric dipole moment. Furthermore, we also discuss other constraints on the charged-Higgs-fermion couplings coming from measurements of $B^0 - \bar{B}^0$ mixing, ρ_0 , and R_b . [S0556-2821(99)02911-2]

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I. INTRODUCTION

One of the most popular extensions of the standard model (SM) is the two-Higgs-doublet model (2HDM) [1], which has two complex Higgs doublets instead of only one in the SM. The 2HDM allows flavor-changing neutral currents (FCNC), which can be avoided by imposing an ad hoc discrete symmetry [2]. One possibility to avoid the FCNC is to couple the fermions only to one of the two Higgs doublets, which is often known as model I. Another possibility is to couple the first Higgs doublet to the down-type quarks while the second Higgs doublet is coupled to the up-type quarks, which is known as model II. Model II has been very popular because it is the building block of the minimal supersymmetric standard model. The physical content of the Higgs sector includes a pair of CP-even neutral Higgs bosons H^0 and h^0 , a CP-odd neutral boson A, and a pair of charged Higgs bosons H^{\pm} .

Models I and II have been extensively studied in literature and tested experimentally. One of the most stringent tests is the radiative decay of B mesons, specifically, the inclusive decay rate of $b \rightarrow s \gamma$, which has the least hadronic uncertainties. The SM rate of $b \rightarrow s \gamma$ including the improved leading-order logarithmic QCD corrections is predicted [3] to be $(2.8\pm0.8)\times10^{-4}$, of which the uncertainty mainly comes from the factorization scale and from the next-to-leading order corrections. In the 2HDM, the rate of $b \rightarrow s \gamma$ can be

enhanced substantially for large regions in the parameter space of the mass $M_{H^{\pm}}$ of the charged-Higgs boson and $\tan \beta = v_2/v_1$, where v_1 and v_2 are the vacuum expectation values of the two Higgs doublets. CLEO published a result of $b \rightarrow s \gamma$ inclusive rate of $(2.32 \pm 0.57 \pm 0.35) \times 10^{-4}$ in 1995 [5], which is recently updated to $[3.15\pm0.35(\text{stat})]$ ± 0.32 (syst) ± 0.26 (mod)] $\times 10^{-4}$ in 1998 [6]. ALEPH also published a result of $[3.11\pm0.80\,(\text{stat})\pm0.72\,(\text{syst})]$ $\times 10^{-4}$ [7]. The 95% C.L. limit published by CLEO is also updated to $2 \times 10^{-4} < B(b \to s \gamma) < 4.5 \times 10^{-4}$ [6]. The data are now more consistent with the SM prediction than before. Hence, the experimental result puts a rather stringent constraint on the charged-Higgs-boson mass $M_{H^{\pm}}$ and $\tan \beta$. In model II, the constraint is $M_{H^{\pm}} \gtrsim 350$ GeV for tan β larger than 1, and even stronger for smaller $\tan \beta$ [8]. However, in model I the constraint is weaker because of possible destructive or constructive interferences with the SM amplitude, depending on $\tan \beta$ and charged-Higgs mass.

Recently, there have been some studies [9,10] on a more general 2HDM without the discrete symmetries as in models I and II. It is often referred as model III. FCNC's in general exist in model III. However, the FCNC's involving the first two generations are highly suppressed from low-energy experiments, and those involving the third generation are not as severely suppressed as the first two generations. It implies that model III should be parametrized in a way to suppress the tree-level FCNC couplings of the first two generations while the tree-level FCNC couplings involving the third generation can be made nonzero as long as they do not violate any existing experimental data, e.g., $B^0 - \bar{B}^0$ mixing.

In this work, we simply assume all tree-level FCNC couplings to be negligible, even though in such a simple model the couplings involving Higgs bosons and fermions can have complex phases $e^{i\theta}$. The effects of such extra phases in $b \rightarrow s \gamma$ have been noticed in Ref. [11]. In this paper, we shall

 $^{^{1}}$ The next leading order (NLO) calculations for the SM and 2HDM I and II are available very recently [4]. The SM result is $(3.29\pm0.33)\times10^{-4}$, which is consistent with the LO calculation. However, the NLO calculation is not available for 2HDM III and, therefore, we will use the LO result consistently throughout the paper.

study carefully the constraint on the phase angle in the product, $\lambda_{tt}\lambda_{bb}$, of Higgs-fermion couplings (see below) versus the mass of the charged Higgs boson from the CLEO data of $b \rightarrow s \gamma$. We shall show that in the calculation of $b \rightarrow s \gamma$ the charged-Higgs amplitude interferes destructively or constructively with the SM amplitude depending crucially on this phase angle and less on the charged-Higgs mass. The usual models I and II are special cases in our study. We shall also show that the previous constraints on the charged-Higgs mass and $\tan \beta$ of model II imposed by the CLEO data can be relaxed in model III because of the presence of this extra phase angle. There are other processes in which the effects of the phase angle can be seen. One of these that we study in this paper is the neutron electric dipole moment. In addition, we also discuss the constraints from experimental measurements of $B^0 - \overline{B}^0$ mixing, ρ_0 , and R_h .

The organization is as follows. In the next section we describe the content of the general 2HDM and write down the Feynman rules for model III. In Sec. III, we describe briefly the effective Hamiltonian formulation for the decay of $b \rightarrow s \gamma$ and derive the Wilson coefficients in model III. We present our numerical results for $b \rightarrow s \gamma$ and study the case of neutron electric dipole moment in Sec. IV. In Sec V, we discuss other experimental constraints from measurements of $B^0 - \overline{B}^0$ mixing, ρ_0 , and R_b . Finally, we conclude in Sec. VI.

II. THE GENERAL TWO-HIGGS-DOUBLET MODEL

In a general two-Higgs-doublet model, both the doublets can couple to the up-type and down-type quarks. Without loss of generosity, we work in a basis such that the first doublet generates all the gauge-boson and fermion masses:

$$\langle \phi_1 \rangle = \begin{pmatrix} 0 \\ \frac{v}{\sqrt{2}} \end{pmatrix}, \langle \phi_2 \rangle = 0,$$
 (1)

where v is related to the W mass by $M_W = (g/2)v$. In this basis, the first doublet ϕ_1 is the same as the SM doublet, while all the new Higgs fields come from the second doublet ϕ_2 . They are written as

$$\phi_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2}G^+ \\ v + \chi_1^0 + iG^0 \end{pmatrix}, \quad \phi_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2}H^+ \\ \chi_2^0 + iA^0 \end{pmatrix}, \quad (2)$$

where G^0 and G^\pm are the Goldstone bosons that would be eaten away in the Higgs mechanism to become the longitudinal components of the weak gauge bosons. The H^\pm are the physical charged-Higgs bosons and A^0 is the physical CP-odd neutral Higgs boson. The χ^0_1 and χ^0_2 are not physical mass eigenstates but linear combinations of the CP-even neutral Higgs bosons:

$$\chi_1^0 = H^0 \cos \alpha - h^0 \sin \alpha, \tag{3}$$

$$\chi_2^0 = H^0 \sin \alpha + h^0 \cos \alpha, \tag{4}$$

where α is the mixing angle. In this basis, there are no couplings of $\chi_2^0 ZZ$ and $\chi_2^0 W^+ W^-$. We can write down [10] the Yukawa Lagrangian for model III as

$$-\mathcal{L}_{Y} = \eta_{ij}^{U} \bar{Q}_{iL} \tilde{\phi}_{1} U_{jR} + \eta_{ij}^{D} \bar{Q}_{iL} \phi_{1} D_{jR}$$

$$+ \xi_{ij}^{U} \bar{Q}_{iL} \tilde{\phi}_{2} U_{jR} + \xi_{ij}^{D} \bar{Q}_{iL} \phi_{2} D_{jR} + \text{H.c.}, \qquad (5)$$

where i,j are generation indices, $\tilde{\phi}_{1,2} = i\sigma_2\phi_{1,2}$, $\eta_{ij}^{U,D}$ and $\xi_{ij}^{U,D}$ are, in general, nondiagonal coupling matrices, and Q_{iL} is the left-handed fermion doublet and U_{jR} and D_{jR} are the right-handed singlets. Note that these Q_{iL} , U_{jR} , and D_{jR} are weak eigenstates, which can be rotated into mass eigenstates. As we have mentioned above, ϕ_1 generates all the fermion masses and, therefore, $(v/\sqrt{2})\eta^{U,D}$ will become the up- and down-type quark-mass matrices after a bi-unitary transformation. After the transformation the Yukawa Lagrangian becomes

$$\mathcal{L}_{Y} = -\bar{U}M_{U}U - \bar{D}M_{D}D - \frac{g}{2M_{W}}(H^{0}\cos\alpha - h^{0}\sin\alpha)(\bar{U}M_{U}U + \bar{D}M_{D}D) + \frac{ig}{2M_{W}}G^{0}(\bar{U}M_{U}\gamma^{5}U - \bar{D}M_{D}\gamma^{5}D)$$

$$+ \frac{g}{\sqrt{2}M_{W}}G^{-}\bar{D}V_{\text{CKM}}^{\dagger}[M_{U^{\frac{1}{2}}}(1 + \gamma^{5}) - M_{D^{\frac{1}{2}}}(1 - \gamma^{5})]U - \frac{g}{\sqrt{2}M_{W}}G^{+}\bar{U}V_{\text{CKM}}[M_{D^{\frac{1}{2}}}(1 + \gamma^{5}) - M_{U^{\frac{1}{2}}}(1 - \gamma^{5})]D$$

$$- \frac{H^{0}\sin\alpha + h^{0}\cos\alpha}{\sqrt{2}}\{\bar{U}[\hat{\xi}^{U}_{\frac{1}{2}}(1 + \gamma^{5}) + \hat{\xi}^{U^{\dagger}}_{\frac{1}{2}}(1 - \gamma^{5})]U + \bar{D}[\hat{\xi}^{D}_{\frac{1}{2}}(1 + \gamma^{5}) + \hat{\xi}^{D^{\dagger}}_{\frac{1}{2}}(1 - \gamma^{5})]D\}$$

$$+ \frac{iA^{0}}{\sqrt{2}}\{\bar{U}[\hat{\xi}^{U}_{\frac{1}{2}}(1 + \gamma^{5}) - \hat{\xi}^{U^{\dagger}}_{\frac{1}{2}}(1 - \gamma^{5})]U - \bar{D}[\hat{\xi}^{D}_{\frac{1}{2}}(1 + \gamma^{5}) - \hat{\xi}^{D^{\dagger}}_{\frac{1}{2}}(1 - \gamma^{5})]D\}$$

$$- H^{+}\bar{U}[V_{\text{CKM}}\hat{\xi}^{D}_{\frac{1}{2}}(1 + \gamma^{5}) - \hat{\xi}^{U^{\dagger}}V_{\text{CKM}^{\frac{1}{2}}}(1 - \gamma^{5})]D - H^{-}\bar{D}[\hat{\xi}^{D^{\dagger}}V_{\text{CKM}^{\frac{1}{2}}}(1 - \gamma^{5}) - V_{\text{CKM}}^{\dagger}\hat{\xi}^{U}_{\frac{1}{2}}(1 + \gamma^{5})]U, \tag{6}$$

where U represents the mass eigenstates of u,c,t quarks and D represents the mass eigenstates of d,s,b quarks. The transformations are defined by $M_{U,D} = \operatorname{diag}(m_{u,d},m_{c,s},m_{t,b}) = (v/\sqrt{2})(\mathcal{L}_{U,D})^{\dagger} \eta^{U,D}(\mathcal{R}_{U,D}), \quad \hat{\xi}^{U,D} = (\mathcal{L}_{U,D})^{\dagger} \xi^{U,D}(\mathcal{R}_{U,D}).$ The Cabibbo-Kobayashi-Maskawa matrix [12] is $V_{\text{CKM}} = (\mathcal{L}_U)^{\dagger}(\mathcal{L}_D)$.

The FCNC couplings are contained in the matrices $\hat{\xi}^{U,D}$. A simple ansatz for $\hat{\xi}^{U,D}$ would be [9]

$$\hat{\xi}_{ij}^{U,D} = \lambda_{ij} \frac{g \sqrt{m_i m_j}}{\sqrt{2} M_W} \tag{7}$$

by which the quark-mass hierarchy ensures that the FCNC within the first two generations are naturally suppressed by the small quark masses, while a larger freedom is allowed for the FCNC involving the third generations. Here λ_{ii} 's are of order O(1) and unlike previous studies [9,10] they can be complex, which give nontrivial consequences different from previous analyses based on models I and II. An interesting example would be the inclusive rate of $b \rightarrow s \gamma$ that we shall study next. Such complex λ_{ii} 's allow the charged-Higgs amplitude to interfere destructively or constructively with the SM amplitude. As we have mentioned, models I and II are special cases in our study and so the previous constraints [8] imposed on the charged-Higgs-boson mass and $\tan \beta$ by the CLEO data can be relaxed by the presence of the extra phase angle. Other interesting phenomenology of the complex λ_{ii} 's includes the electric dipole moments of electrons and quarks [13] as a consequence of the explicit *CP* violation due to the complex phase in the charged-Higgs sector. For simplicity we choose $\hat{\xi}^{U,D}$ to be diagonal to suppress all tree-level FCNC couplings and, consequently, the λ_{ii} 's are also diagonal but remain complex. Such a simple scenario is sufficient to demonstrate our claims.

III. INCLUSIVE $B \rightarrow X_s \gamma$

The detailed description of the effective Hamiltonian approach can be found in Refs. [3,14]. Here we present the highlights that are relevant to our discussions. The effective Hamiltonian for $B \rightarrow X_s \gamma$ at a factorization scale of order $O(m_b)$ is given by

$$\mathcal{H}_{\text{eff}} = -\frac{G_F}{\sqrt{2}} V_{ts}^* V_{tb} \left[\sum_{i=1}^6 C_i(\mu) Q_i(\mu) + C_{7\gamma}(\mu) Q_{7\gamma}(\mu) + C_{8G}(\mu) Q_{8G}(\mu) \right]. \tag{8}$$

The operators Q_i can be found in Ref. [3], of which the Q_1 and Q_2 are the current-current operators and $Q_3 - Q_6$ are QCD penguin operators. $Q_{7\gamma}$ and Q_{8G} are, respectively, the magnetic penguin operators specific for $b \rightarrow s \gamma$ and $b \rightarrow s g$. Here we also neglect the mass of the external strange quark compared to the external bottom-quark mass.

The factorization in Eq. (8) facilitates the separation of the short-distance and long-distance parts, of which the short-distance parts correspond to the Wilson coefficients C_i and are calculable by perturbation while the long-distance parts correspond to the operator matrix elements. The physical quantities based on Eq. (8) should be independent of the factorization scale μ . The natural scale for factorization is of order m_b for the decay $B \rightarrow X_s \gamma$. The calculation of the $C_i(\mu)$'s divides into two separate steps. First, at the electroweak scale, say M_W , the full theory is matched onto the effective theory and the coefficients $C_i(M_W)$ at the W-mass scale are extracted in the matching process. In a while, we shall present these coefficients $C_i(M_W)$ in model III. Second, the coefficients $C_i(M_W)$ at the W-mass scale are evolved down to the bottom-mass scale using renormalization group equations. Since the operators Q_i 's are all mixed under renormalization, the renormalization group equations for C_i 's are a set of coupled equations:

$$\vec{C}(\mu) = U(\mu, M_W) \vec{C}(M_W), \tag{9}$$

where $U(\mu, M_W)$ is the evolution matrix and $\tilde{C}(\mu)$ is the vector consisting of $C_i(\mu)$'s. The calculation of the entries of the evolution matrix U is nontrivial but it has been written down completely in the leading order [3]. The coefficients $C_i(\mu)$ at the scale $O(m_b)$ are given by [3]

$$C_j(\mu) = \sum_{i=1}^8 k_{ji} \eta^{a_i} \ (j=1,\ldots,6),$$
 (10)

$$C_{7\gamma}(\mu) = \eta^{16/23} C_{7\gamma}(M_W) + \frac{8}{3} (\eta^{14/23} - \eta^{16/23}) C_{8G}(M_W) + C_2(M_W) \sum_{i=1}^{8} h_i \eta^{a_i},$$
(11)

$$C_{8G}(\mu) = \eta^{14/23} C_{8G}(M_W) + C_2(M_W) \sum_{i=1}^{8} \bar{h}_i \eta^{a_i}, \tag{12}$$

with $\eta = \alpha_s(M_W)/\alpha_s(\mu)$. The a_i 's, k_{ji} 's, h_i 's, and \bar{h}_i 's can be found in Ref. [3].

Once we have all the Wilson coefficients at the scale $O(m_b)$ we can then compute the decay rate of $B \rightarrow X_s \gamma$. The decay amplitude for $B \rightarrow X_s \gamma$ is given by

$$\mathcal{A}(B \to X_s \gamma) = -\frac{G_F}{\sqrt{2}} V_{ts}^* V_{tb} C_{7\gamma}(\mu) \langle Q_{7\gamma} \rangle, \qquad (13)$$

in which we use the spectator approximation to evaluate the matrix element $\langle Q_{7\gamma} \rangle$ and $m_B{\simeq}m_b$. The decay rate of $B \to X_s \gamma$ is given by

$$\Gamma(B \to X_s \gamma) = \frac{G_F^2 |V_{ts}^* V_{tb}|^2 \alpha_{\text{em}} m_b^5}{32 \pi^4} |C_{7\gamma}(m_b)|^2, \quad (14)$$

where $C_{7\gamma}(m_b)$ is given in Eq. (11). Since this decay rate depends on the fifth power of m_b , a small uncertainty in the choice of m_b will create a large uncertainty in the decay rate, therefore, the decay rate of $B \rightarrow X_s \gamma$ is often normalized to the experimental semileptonic decay rate as

$$\frac{\Gamma(B \to X_s \gamma)}{\Gamma(B \to X_c e \bar{\nu}_e)} = \frac{|V_{ts}^* V_{tb}|^2}{|V_{cb}|^2} \frac{6 \alpha_{\text{em}}}{\pi f(m_c/m_b)} |C_{7\gamma}(m_b)|^2,$$
(15)

where
$$f(z) = 1 - 8z^2 + 8z^6 - z^8 - 24z^4 \ln z$$
.

The remaining task is the calculation of the Wilson coefficients $C_i(M_W)$ at the W-mass scale. The necessary Feynman rules can be obtained from the Lagrangian in Eq. (6). As we have mentioned, we assume all tree-level FCNC couplings negligible and, therefore, the neutral-Higgs bosons do not contribute at tree level or at one-loop level. The only contributions at one-loop level come from the charged-Higgs bosons H^\pm , the charged Goldstone bosons G^\pm , and the SM W^\pm bosons.

The coefficients $C_i(M_W)$ at the leading order in model III are given by

$$C_i(M_W) = 0 \quad (j = 1, 3, 4, 5, 6),$$
 (16)

$$C_2(M_W) = 1,$$
 (17)

$$C_{7\gamma}(M_W) = -\frac{A(x_t)}{2} - \frac{A(y)}{6} |\lambda_{tt}|^2 + B(y)\lambda_{tt}\lambda_{bb},$$
 (18)

$$C_{8G}(M_W) = -\frac{D(x_t)}{2} - \frac{D(y)}{6} |\lambda_{tt}|^2 + E(y)\lambda_{tt}\lambda_{bb},$$
(19)

where $x_t = m_t^2/M_W^2$, and $y = m_t^2/M_{H^{\pm}}^2$. The Inami-Lim functions [15] are given by

$$A(x) = x \left[\frac{8x^2 + 5x - 7}{12(x - 1)^3} - \frac{(3x^2 - 2x)\ln x}{2(x - 1)^4} \right], \tag{20}$$

$$B(y) = y \left[\frac{5y - 3}{12(y - 1)^2} - \frac{(3y - 2)\ln y}{6(y - 1)^3} \right],\tag{21}$$

$$D(x) = x \left[\frac{x^2 - 5x - 2}{4(x - 1)^3} + \frac{3x \ln x}{2(x - 1)^4} \right],$$
 (22)

$$E(y) = y \left[\frac{y-3}{4(y-1)^2} + \frac{\ln y}{2(y-1)^3} \right]. \tag{23}$$

The SM results for the Wilson coefficients $C_i(M_W)$ for $i=1,\ldots,6$ are the same as in Eqs. (16) and (17), while $C_{7\gamma}(M_W)$ and $C_{8G}(M_W)$ only have the first term as in Eqs. (18) and (19), respectively. Thus, we already have all the necessary pieces to compute the decay rate of $B \rightarrow X_s \gamma$.

Before we leave this section we would like to emphasize that the expressions for $C_i(M_W)$ in Eqs. (16)–(19) obtained for model III can be reduced to the results of models I and II by the following substitutions:

$$\lambda_{tt} \rightarrow \cot \beta$$
 and $\lambda_{bb} \rightarrow \cot \beta$ (for model I), (24)

and

$$\lambda_{tt} \rightarrow \cot \beta$$
 and $\lambda_{bb} \rightarrow -\tan \beta$ (for model II). (25)

IV. RESULTS

We use the following inputs [3,16,17] for our calculation: m_t = 173.8 GeV, M_W = 80.388 GeV, $|V_{ts}^*V_{tb}|^2/|V_{cb}|^2$ = 0.95, m_c/m_b = 0.3, and $B(b\to ce^{-\nu})$ = 10.45 \pm 0.21%, $\alpha_{\rm em}(m_b)$ \approx 1/133, and $\alpha_s(M_Z)$ = 0.119 and a 1-loop α_s is employed. The branching ratio $B(B\to X_s\gamma)$ is calculated using Eq. (15). The free parameters are then M_{H^\pm} , λ_{tt} , and λ_{bb} , as in Eqs. (18) and (19).

Since the term proportional to $\lambda_{tt}\lambda_{bb}$ is, in general, complex we let $\lambda_{tt}\lambda_{bb} = |\lambda_{tt}\lambda_{bb}|e^{i\theta}$. We show the contours of the branching ratio in the plane of θ and $M_{H^{\pm}}$ for $|\lambda_{tt}\lambda_{bb}| = 3,1,0.5$ in Figs. 1(a), 1(b), and 1(c), respectively. The contours are symmetric about $\theta = 180^{\circ}$. The contours are $B = (2,2.8,4.5) \times 10^{-4}$, which correspond to 95% C.L. lower limit, the SM value, and the 95% C.L. upper limit. The value of $|\lambda_{bb}|$ is set at 50 as preferred in the R_b constraint that will be shown in the next section. The corresponding values of $|\lambda_{tt}|$ are 0.06, 0.02, and 0.01, which satisfy the constraint from the $B^0 - \overline{B}^0$ mixing, as will also be discussed in the next section. Here the term proportional to $|\lambda_{tt}|^2$ is not crucial because the coefficient of $|\lambda_{tt}|^2$ is small compared with the other two terms in Eqs. (18) and (19).

The results of the conventional model II (which can be obtained from our general results by the substitution: λ_{tt} $\rightarrow \cot \beta$, $\lambda_{bb} \rightarrow -\tan \beta$) can be read off from Fig. 1(b) at θ = 180°. The $b \rightarrow s \gamma$ data severely constrain $M_{H^{\pm}} \gtrsim 350 \text{ GeV}$ at 95% C.L. level, because at θ = 180° the SM amplitude interferes entirely constructively with the charged Higgsboson amplitude. It is obvious that at other angles the mass of the charged Higgs-boson mass is less constrained; especially, in the range $\theta = 50^{\circ} - 90^{\circ}$ the entire range of charged Higgs-boson mass is allowed by the $b \rightarrow s \gamma$ constraint as long as $|\lambda_{tt}\lambda_{bb}| \leq 1$. However, when $|\lambda_{tt}\lambda_{bb}|$ is getting larger, say 3 [see Fig. 1(a)], the allowed range of charged Higgs-boson mass becomes narrow. This is because the charged Higgs-boson amplitude becomes too large compared with the SM amplitude. On the other hand, when $|\lambda_{tt}\lambda_{bb}|$ becomes small the allowed range charged Higgs-boson mass is enlarged, as shown in Fig. 1(c). The significance of the phase angle θ is that the constraints previously on $M_{H^{\pm}}$ and $\tan \beta$ are evolved into θ , $M_{H^{\pm}}$, λ_{tt} , and λ_{bb} , where we do not need to impose $|\lambda_{tt}| = 1/|\lambda_{bb}|$, as in model II. The previous tight constraint on $M_{H^{\pm}}$ of model II is now relaxed in model III down to virtually the direct search limit of almost 60 GeV at the CERN e^+e^- collider LEPII [18].

The phase θ of $\lambda_{tt}\lambda_{bb}$ can give rise to the neutron electric dipole moment (NEDM). The physics involved can be understood as follows. First, at the electroweak scale the phase θ induces the CP violating color dipole moment (CDM) of the b quark. Second, the CDM of b quark evolves by renormalization to the scale at m_b and turns into the Weinberg operator [19] (i.e., the gluonic CDM [20]) when the b-quark

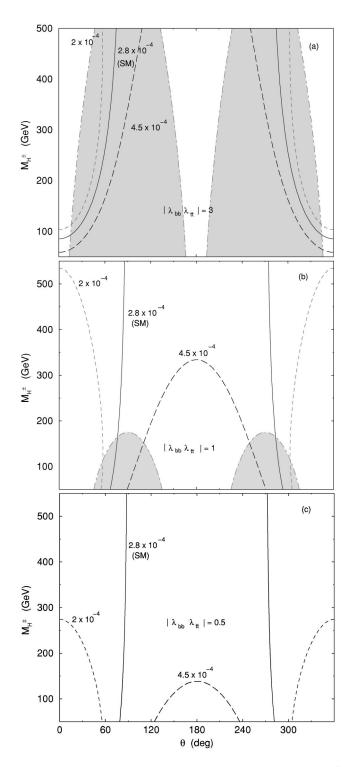


FIG. 1. Contour plot of the branching ratio $b \rightarrow s \gamma$ versus M_H^{\pm} and the phase of $\lambda_{tt}\lambda_{bb}$ for various values of $|\lambda_{tt}\lambda_{bb}| = 3,1,0.5$. The shaded areas are excluded by the NEDM constraint $|d_n| < 10^{-25}$ e·cm.

field is integrated away. Finally, this gives NEDM at the nucleon mass scale:

$$d_n^g = g_s^3(\mu) C_g(\mu) \langle \mathcal{O}_g(\mu) \rangle,$$

where

$$\mathcal{O}_{g} = \frac{1}{6} f^{abc} \varepsilon^{\delta \nu \alpha \beta} G^{a}_{\alpha \beta} G^{b}_{\lambda \delta} G^{c}_{\lambda \nu}. \tag{26}$$

Weinberg suggested the hadronic scale μ to be set at the value such that $g_s(\mu) = 4\pi/\sqrt{6}$. Instead we choose μ at the nucleon mass. The hadronic matrix element $\langle \mathcal{O}_g(\mu) \rangle$ is very uncertain. A typical estimate from the naive dimension analysis (NDA) [21] relates the matrix element to the chiral symmetry breaking scale $M_{\nu} = 2\pi F_{\pi} = 1.19$ GeV,

$$\mathcal{O}_{g} = \frac{eM_{\chi}}{4\pi} \, \xi_{g}(\mu). \tag{27}$$

The parameter ξ_g is set to be 1 in NDA, but other calculations result in different ξ_g . QCD sum rule performed by Chemtob [22] gives $\xi_g = 0.07$. Scaling argument by Bigi and Uraltsev [23] yields a value $\xi_g = 0.03$. We choose $\xi_g = 0.1$ for our analysis. The Wilson coefficient of the Weinberg operator C_g evolves according to the renormalization group (RG) equation [24] and matches [25,26] that induced by the CDM C_b of the b quark at the scale m_b . Our definitions of Wilson coefficients follow the notation in Ref. [26],

$$C_g(\mu) = \frac{1}{32\pi^2} C_b(m_b) \left(\frac{\alpha_s(m_b)}{\alpha_s(m_c)} \right)^{54/25} \left(\frac{\alpha_s(m_c)}{\alpha_s(\mu)} \right)^{54/27}.$$
(28)

The CDM of the b quark comes from the CP violation of the charged Higgs coupling at the electroweak scale and at the scale m_b it is given by

$$C_b(m_b) = \frac{\sqrt{2}G_F}{16\pi^2} \operatorname{Im} \left(\lambda_{tt}\lambda_{bb}\right) \frac{2}{3} H\left(\frac{m_t^2}{M_{H^{\pm}}^2}\right) \left(\frac{\alpha_s(m_W)}{\alpha_s(m_b)}\right)^{14/23},\tag{29}$$

where the function H is

$$H(y) = \frac{3}{2} \frac{y}{(1-y)^2} \left(y - 3 - \frac{2\log gy}{1-y} \right). \tag{30}$$

Note that H(1)=1 when $M_{H^{\pm}}=m_t$. Numerically,

$$d_n^g = 10^{-25} e \cdot \operatorname{cm} \operatorname{Im} \left(\lambda_{tt} \lambda_{bb} \right) \left(\frac{\alpha(m_n)}{\alpha(\mu)} \right)^{1/2} \left(\frac{\xi_g}{0.1} \right) H \left(\frac{m_t^2}{M_{H^{\pm}}^2} \right). \tag{31}$$

The experimental limit,

$$d_n < 10^{-25} \text{e} \cdot \text{cm},$$
 (32)

places an upper bound $|\operatorname{Im}(\lambda_{tt}\lambda_{bb})| \leq 1$ on the coupling product for our choice of parameters, $\xi_g = 0.1$, $\mu = m_n$ when $M_{H^{\pm}} \approx m_t$. The bound is sensitive to uncertainties in μ and ξ_g , but not much in $M_{H^{\pm}}$. The function value H decreases only by a factor of 1.6 as the charged Higgs mass varies from 50 GeV to 200 GeV.

In Fig. 1, the constraint on the M_{H^\pm} versus θ is given by the shaded areas which are excluded by the NEDM measurement.

For the case of rather large $|\lambda_{tt}\lambda_{bb}| \gg 1$, the phase becomes restricted to the forward region $\theta \sim 0$ or the backward region π . However, the backward region $(\theta \sim \pi)$ is not pref-

erable for $M_{H^{\pm}} \lesssim 500$ GeV due to the constraint from $b \to s \gamma$. If the charged Higgs boson is this light with large couplings to the b and t quarks, the NEDM analysis requires a small phase in the forward region. On the other hand, when $|\lambda_{tt}\lambda_{bb}| < 0.7$, the NEDM constraint becomes ineffective and the constraint from $b \to s \gamma$ remains useful.

Other places to look for the effects of this angle θ include other $b \rightarrow s, d$ decays, CP violation effects in $b \rightarrow s \gamma$ [11], $b \rightarrow s l \bar{l}$, and the electric dipole moments of fermions via a 2-loop mechanism [13].

On the other hand, this phase angle θ will not show up in other existing constraints like ρ_0 , R_b , and flavor-mixing. The previous argument that the 2HDM only has a very narrow window left to accommodate all the constraints from $B(b \rightarrow s \gamma)$, ρ_0 , R_b , and flavor-mixing is now not true because of the possible phase angle in model III that we are considering. The narrow window on M_{H^\pm} opens up. We shall summarize the other constraints on λ_{tt} , λ_{bb} , and Higgs masses in the next section.

V. OTHER CONSTRAINTS

Direct searches for Higgs bosons in 2HDM at LEPII [18] place the following limits on Higgs boson masses:

$$M_{h^0} > 77$$
 GeV, $M_A > 78$ GeV, $M_{H^{\pm}} > 56 - 59$ GeV, (33)

where the M_{h^0} and M_A mass limits are obtained by combining the four LEP experiments but no combined limit on M_{H^\pm} is available [18]. We shall then discuss other constraints from precision measurements.

A.
$$K^0 - \bar{K}^0$$
. $D^0 - \bar{D}^0$, and $B^0 - \bar{B}^0$

These $F^0 - \bar{F}^0$ (F = K, D, B) flavor-mixing processes can occur via tree-level, penguin, and box diagrams in model III [10]. One particular argument against model III is that it allows FCNC at the tree level, but with a lot of freedom in picking the parameters λ_{ij} it certainly survives all the present FCNC constraints. The tree-level diagrams for these ΔF = 2 processes can be eliminated by choosing λ_{ui} , λ_{di} very small. Actually, in our study we have set $\lambda_{ii} = 0$ $(i \neq j)$; therefore, all tree-level FCNC diagrams are eliminated and so are the penguin diagrams. However, there are important contributions coming from the box diagrams with the charged Higgs boson. Naively, to suppress the charged Higgs contribution we need to increase the charged Higgs boson mass or decrease λ_{tt} . We shall obtain a set of bounds using the experimental measurement x_d of $B^0 - \bar{B}^0$ in the following $[K^0 - \bar{K}^0]$ and $D^0 - \bar{D}^0$ mixings are small in our model because of the mass hierarchy choice of $\hat{\xi}_{ii}^{U,D}$ in Eq. (7)].

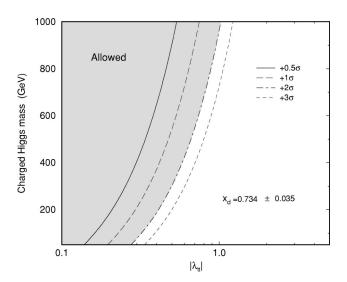


FIG. 2. Contour plot of the $B^0 - \overline{B}^0$ mixing parameter x_d in the plane of $|\lambda_{tt}|$ and the charged Higgs boson mass. The experimental value is $x_d = 0.734 \pm 0.035$.

The quantity that parametrizes the $B^0 - \overline{B}^0$ mixing is

$$x_{d} = \frac{\Delta m_{B}}{\Gamma_{B}}$$

$$= \frac{G_{F}^{2}}{6\pi^{2}} |V_{td}^{*}|^{2} |V_{tb}|^{2} f_{B}^{2} B_{B} m_{B} \eta_{B} \tau_{B} M_{W}^{2} (I_{WW} + I_{WH} + I_{HH})$$
(34)

where [27]

$$\begin{split} I_{WW} &= \frac{x}{4} \left[1 + \frac{3 - 9x}{(x - 1)^2} + \frac{6x^2 \log x}{(x - 1)^3} \right], \\ I_{WH} &= xy |\lambda_{tt}|^2 \left[\frac{(4z - 1) \log y}{2(1 - y)^2(1 - z)} - \frac{3 \log x}{2(1 - x)^2(1 - z)} + \frac{x - 4}{2(1 - x)(1 - y)} \right], \\ I_{HH} &= \frac{xy |\lambda_{tt}|^4}{4} \left[\frac{1 + y}{(1 - y)^2} + \frac{2y \log y}{(1 - y)^3} \right], \end{split}$$

where $x=m_t^2/M_W^2$, $y=m_t^2/M_{H^\pm}^2$, $z=M_W^2/M_{H^\pm}^2$, and the running top mass $m_t=m_t(m_t)=166$ GeV. We use these inputs [17,16,3]: $|V_{tb}|=1$, $f_B^2B_B=(0.175 \text{ GeV})^2(1.4)$, $m_B=5.2798$ GeV, $\eta_B=0.55$, and $x_d=0.734\pm0.035$, $\tau_B=1.56$ ps. Since the allowable range of $|V_{td}|$ is from 0.004 to 0.013 [17], we use a central value for $|V_{td}|$ obtained using the central value of x_d and it gives $|V_{td}|\approx0.0084$ (which is the central value given in the Particle Data Group book 98 [17]). We then obtain bounds on λ_{tt} and M_{H^\pm} by the 2σ limit of x_d assuming the only error comes from x_d measurement (see Fig. 2):

$$M_{H^{\pm}} \gtrsim 77$$
 (60) GeV for $|\lambda_{tt}| \lesssim 0.3$ (0.28), (35)

which means virtually no limit on the charged Higgs boson mass if $|\lambda_{tt}| \le 0.28$, because the present direct search limit on charged Higgs boson is about 56–59 GeV [Eq. (33)]. We have improved the results in Refs. [28,10] because we are using an updated value of x_d . In the context of models I and II the bound is $M_{H^\pm} \ge 77(60)$ GeV for $\tan \beta \ge 3.3(3.6)$. For $\tan \beta$ gets close to 1, $M_{H^\pm} > 1$ TeV.

B. ρ_0

 ρ was introduced to measure the relation between the masses of W and Z bosons. In the SM $\rho = M_W^2/M_Z^2\cos\theta_{\rm w}$ = 1 at the tree level. However, the ρ parameter receives contributions from the SM corrections and from new physics. The deviation from the SM predictions is usually described by the parameter ρ_0 defined by [16]

$$\rho_0 = \frac{M_W^2}{\rho M_Z^2 \cos^2 \theta_{\rm w}},\tag{36}$$

where the ρ in the denominator absorbs all the SM corrections, among which the most important SM correction at 1-loop level comes from the heavy top-quark:

$$\rho \simeq 1 + \Delta \rho_{\text{top}} = 1 + \frac{3G_F}{8\sqrt{2}\pi^2} m_t^2, \qquad (37)$$

in which $\Delta \rho_{\text{top}}$ is about 0.0095 for m_t = 173.8 GeV. By definition ρ_0 =1 in the SM. The reported value of ρ_0 is [16]

$$\rho_0 = 0.9996^{+0.0017}_{-0.0013} \ (2\sigma). \tag{38}$$

In terms of new physics (2HDM here) the constraint becomes

$$-0.0017 < \Delta \rho_{2\text{HDM}} < 0.0013. \tag{39}$$

In 2HDM ρ_0 receives contribution from the Higgs bosons given by, in the context of model III [28,29,10],

$$\Delta \rho_{2\text{HDM}} = \frac{G_F}{8\sqrt{2}\pi^2} \left[\sin^2 \alpha F(M_{H^{\pm}}, M_A, M_{H^0}) + \cos^2 \alpha F(M_{H^{\pm}}, M_A, M_{h^0}) \right], \tag{40}$$

where

$$\begin{split} F(m_1, m_2, m_3) &= m_1^2 - \frac{m_1^2 m_2^2}{m_1^2 - m_2^2} \log \left(\frac{m_1^2}{m_2^2} \right) \\ &- \frac{m_1^2 m_3^2}{m_1^2 - m_3^2} \log \left(\frac{m_1^2}{m_3^2} \right) \\ &+ \frac{m_2^2 m_3^2}{m_2^2 - m_3^2} \log \left(\frac{m_3^2}{m_3^2} \right). \end{split}$$

Since ρ_0 is constrained to be around 1 we have to minimize the contributions of $\Delta \rho_{\rm 2HDM}$. Without loss of generosity we set $\alpha = 0$, which means that the heavier neutral Higgs H^0 decouples and the first Higgs doublet can be identified as the SM Higgs doublet, while the second Higgs doublet is the source of new physics. The leading behavior of $\Delta \rho_{\rm 2HDM}$ scale as $M_{H^\pm}^2$ and, therefore, the constraint of ρ_0 in Eq. (38) puts an upper bound on M_{H^\pm} . Actually, if the charged Higgs mass M_{H^\pm} is between M_A and M_{h^0} the $\Delta \rho_{\rm 2HDM}$ is negative. However, this is not the favorite scenario because in the case of R_b the experimental result prefers $M_A \approx M_{h^0} \approx 80-120$ GeV, that will be discussed in the next subsection. In this case $M_A \approx M_{h^0}$, $\Delta \rho_{\rm 2HDM}$ is positive and, therefore, we want to keep it small. Using Eq. (40) for $M_A \approx M_{h^0} = 80-120$ GeV, the charged Higgs mass is constrained to be

$$M_{H^{\pm}} \lesssim 180 - 220 \text{ GeV}.$$
 (41)

$C. R_h$

 R_b was about $+3.7\sigma$ above the SM value a few years ago, but now the deviation is reduced to $+1\sigma$ after almost all LEP data have been analyzed [16]. $R_b^{\rm exp}$ still places a constraint on the 2HDM, though it is much less severe than before. This is because only a narrow window exists in the neutral Higgs bosons that does not decrease R_b while the charged-Higgs boson always decreases R_b . We shall divide the discussion into two parts: neutral-Higgs contribution and charged-Higgs contribution.

According to Ref. [29] the contribution from the neutral Higgs boson is positive in a narrow window of 20 GeV $< M_A \approx M_{h^0} < 120$ GeV and is negative otherwise. Since the charged Higgs boson contribution always decreases R_h , it makes more sense to require the neutral Higgs contribution to be positive. Here we adapt the formulas in Ref. [29] to model III. First, the contribution from the neutral Higgs bosons only depends on $|\lambda_{bb}|$ and the masses of the neutral Higgs bosons. Again without loss of generosity, we set the scalar Higgs-boson mixing angle $\alpha = 0$ in order to decouple the heavier H^0 . We show the resultant R_h due to the presence of the neutral Higgs bosons in Fig. 3(a) for $|\lambda_{bb}| = 30,50,70$, where $R_b^{\text{SM}} = 0.2158$, $R_b^{\text{exp}} = 0.21656 \pm 0.00074$ [16], and the 1σ is taken to be the standard deviation of the experimental result. In Fig. 3(a) the horizontal lines represent the R_h^{SM} , $+1\sigma$, and $+2\sigma$ values. The $R_b^{\rm exp}$ is almost at the $+1\sigma$ line. If we allow only 1σ value below R_h^{exp} , we need $M_{h^0} \approx M_A$ $\approx\!80\text{--}120$ GeV with a fairly large $|\lambda_{\mathit{bb}}|.$ For $|\lambda_{\mathit{bb}}|$ as large as 70 the enhancement can be as large as $+1\sigma$ at $M_{H^{\pm}} = 80$ GeV. On the other hand, if we allow 2σ below R_h^{exp} , then we can have all the range of $M_{h^0} \approx M_A > 80$ GeV, as can be seen in Fig. 3(a). At any rate, the preferred scenario is M_{h^0} $\approx M_A = 80-120$ GeV with a fairly large $|\lambda_{bb}|$. How large should $|\lambda_{bb}|$ be? It depends on the charged Higgs contribution as well.

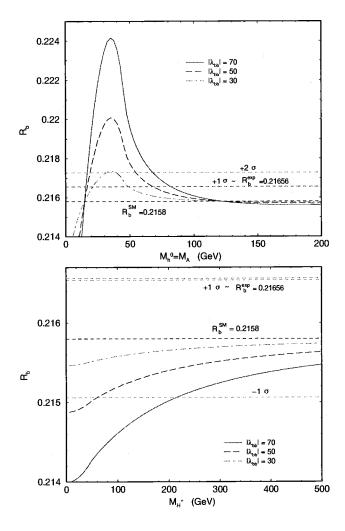


FIG. 3. The $R_b \equiv \Gamma(Z \rightarrow b\bar{b})/\Gamma_{\rm had}$ due to the presence of (a) the neutral Higgs bosons, $M_A \simeq M_{h^0}$ and (b) the charged Higgs boson.

Since the charged Higgs-boson contribution is always negative, we want to make it as small as possible. This contribution depends on $|\lambda_{tt}|, |\lambda_{bb}|,$ and $M_{H^\pm}.$ The effect on R_b due to the presence of the charged Higgs boson is shown in Fig. 3(b) for $|\lambda_{bb}|=30,50,70$ and $|\lambda_{tt}|=0.05$. In Fig. 3(b) the horizontal lines represent the $R_b^{\rm SM}$ and $\pm 1\sigma$. The $R_b^{\rm exp}$ is very close to $\pm 1\sigma$ line. It is clear from the graph that because we do not want the charged Higgs contribution to reduce $R_b^{\rm SM}$ by more than 1σ , we require $M_{H^\pm}{\gtrsim}60$ (220) GeV for $|\lambda_{bb}|=50$ (70).

Since $R_b^{\rm exp}$ is only $+ 1\,\sigma$ away from $R_b^{\rm SM}$, it is not necessary to keep the narrow window of M_A and M_{h^0} if we allow $2\,\sigma$ below the experimental data. In this case, M_{h^0} and M_A can be widened to much larger masses, and so the ρ_0 constraint on the ceiling of the charged Higgs mass will also be relaxed. However, M_{H^\pm} cannot be too small, otherwise R_b will be decreased to an unacceptable value.

Summarizing this section the constraints by $B^0 - \overline{B}^0$ mixing, ρ_0 , and R_b give the following preferred scenario: (1) $M_A \approx M_{h^0} = 80 - 120$ GeV; (2) $|\lambda_{bb}| \approx 50$; (3) $|\lambda_{tt}| \lesssim 0.3$; (4) 80 GeV $\lesssim M_{H^\pm} \lesssim 200$ GeV.

VI. CONCLUSIONS

We have demonstrated that in model III of the general two-Higgs-doublet model the charged-Higgs-fermion couplings can be complex, even in the simplified case of no tree-level FCNC couplings. The phase angle in the complex charged-Higgs-fermion coupling determines the interference between the standard model amplitude and the charged-Higgs amplitude in the process of $b \rightarrow s \gamma$. We found that for $|\lambda_{bb}\lambda_{tt}| \approx 1$ there is a large range of the phase angle ($\theta \approx 50^{\circ} - 90^{\circ}$ and $270^{\circ} - 310^{\circ}$) such that the rate of $b \rightarrow s \gamma$ is within the experimental value for all range of $M_{H^{\pm}}$. In other words, the previous tight constraints on $M_{H^{\pm}}$ of model II from the CLEO $b \rightarrow s \gamma$ rate is relaxed in model III, depending on this phase angle. In addition, we also examined the effect of this phase angle on the neutron electric dipole moment and discussed other experimental constraints on model III. The necessary constraints are already listed at the end of the last section. Here we offer the following comments.

- (1) The phase angle induces a CP-violating chromoelectric dipole moment of the b-quark, which leads to a substantial enhancement in neutron electric dipole moment. The experimental upper limit on neutron electric dipole moment thus places an upper bound on the couplings: $|\lambda_{tt}\lambda_{bb}|\sin\theta \lesssim 0.8$ for $M_{H^\pm} \approx 100$ GeV. This bound has large uncertainties due to the hadronic matrix element of the neutron and the factorization scale.
- (2) The phase angle will also cause other CP-violating effects in other processes, e.g., the decay rate difference between $b \rightarrow s \gamma$ and $\bar{b} \rightarrow \bar{s} \gamma$ [11], and in lepton asymmetries of $b \rightarrow s l^+ l^-$. These processes will soon be measured at the future B factories.
- (3) Other experimental measurements, like $F^0 \overline{F}^0$ mixing, ρ_0 , and R_b , constrain only the magnitude of the couplings and the Higgs-boson masses but not the phase angle.
- (4) The $B^0 \overline{B}^0$ mixing measurement can only constrain the charged-Higgs mass and $|\lambda_{tt}|$ loosely because the mixing parameter x_d depends on $|V_{td}|$, which is not yet well measured. Other uncertainties come from the hadronic factors: f_B , B_B , and η_B . Actually, the mixing parameter x_d is often used to determine $|V_{td}|$.
- (5) As we have mentioned, if $R_b^{\rm SM}$ gets closer to the SM value the constraint on the neutral Higgs-boson masses M_A and $M_{h^0} = 80 120$ GeV will go away completely. On the other hand, the charged-Higgs boson mass is still required to be larger than about 60 GeV (for $|\lambda_{bb}| = 50$) in order not to decrease R_b significantly.

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